$\qquad$

## This booklet consists of 100 questions and 12 printed pages.

RGUPET/ $\qquad$
RGUPET 2023
Ph.D. in STATISTICS

Full Marks: 100

Series
NIL

Time: 3 Hours

Roll No. $\square$

Day and Date of Examination
:

Signature of Invigilator(s)
Signature of Candidate
:

General Instructions:

## please read all the instructions carefully before making any entry.

1. DO NOT OPEN THIS TEST BOOKLET UNTIL YOU ARE TOLD TO DO SO.
2. Candidate must write his/her Roll Number on the space provided.
3. This Test Booklet contains 100 Multiple Choice Questions (MCQs) from the concerned subject. Each question carries 1 mark.
4. Please check the Test Booklet to verify that the total pages and total number of questions contained in the test booklet are the same as those printed on the top of the first page. Also check whether the questions are in sequential order or not.
5. Candidates are not permitted to enter into the examination hall 15 minutes after the commencement of the entrance test or leave the examination hall before 30 minutes of end of examination.
6. Making any identification mark in the OMR Answer Sheet or writing Roll Number anywhere other than the specified places will lead to disqualification of the candidate.
7. Candidates shall maintain silence inside and outside the examination hall. If candidate(s) is/are found violating the instructions mentioned herein or announced in the examination hall, they will be summarily disqualified from the entrance test.
8. In case of any dispute, the decision of the Entrance Test Committee, RGU shall be final and binding.
9. The OMR Answer Sheet consists of two copies, the Original copy and the Student's copy.



| 14 | The correct relation between variance and standard deviation (S.D.) of a variable X is: |  |  |  |  |  |  |  | $\begin{gathered} \text { S.D. }= \\ {[\operatorname{Var}(X)]^{1 / 2}} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a) <br> S.D <br> .= <br> $\operatorname{Var}($ | b)$\text { S.D. }=[\operatorname{Var}(X)]^{2}$ |  | c)$\begin{aligned} & \text { S.D. }= \\ & {[\operatorname{Var}(X)]^{3}} \end{aligned}$ |  | d) S.D. $=[\operatorname{Var}(X)]^{1 / 2}$ |  |  |  |
| 15 | In the case of positively skewed distribution, the extreme values lie in the |  |  |  |  |  |  | c | right tail |
|  | a) <br> left <br> tail | b) middle |  | c) right tail |  | d) does not exist |  |  |  |
| 16 | In the regression line of $Y$ on $X$, the variable $X$ is known as: |  |  |  |  |  |  | a | ```independ ent variable``` |
|  | a) independent variable |  | b) dependent variable |  | c) response variable |  | d) all |  |  |
| 17 | When $\beta_{Y X}$ is the slope for the regression line of Y on X and $\beta_{X Y}$ is the slope for the regression line of $X$ on $Y$. What should be the value of $\beta_{X Y}$ if $\beta_{Y X}>1$ |  |  |  |  |  |  | a | less than 1 |
|  | a) less than 1 |  | b) greater than 1 |  | c) |  | d) equal to 0 |  |  |
| 18 | The range of correlation coefficient is: |  |  |  |  |  |  | d | -1 to 1 |
|  |  |  |  |  |  |  | d) -1 to 1 |  |  |
| 19 | The individual probabilities of occurrence of two events $A$ and $B$ are known, the probability of occurrence of both events together will be |  |  |  |  |  |  | b | decrease <br> d |
|  | a) increased |  | b) decre |  | c) on |  | d) zero |  |  |
| 20 | One of the two events must happen; given that the chance of one is one-fourth of the other. The odd in favour of the other is: |  |  |  |  |  |  | b | 1: 4 |
|  | a) $1: 3$ | 3 b) $1: 4$ |  |  | c) 4 : |  | d) $1: 5$ |  |  |
| 21 | Let $\underline{X} \sim N_{p}(\underline{\mu}, \Sigma)$ and $(\underline{X}-\underline{\mu})^{\prime} \Sigma^{-1}(\underline{X}-\underline{\mu})$ follow the Chi-square distribution with degrees of freedom |  |  |  |  |  |  |  |  |


|  | a)p-1 | b) $p$ | c) $p+1$ |  | d) $p+2$ | b | p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 22 | Suppose $\underline{X}_{1}, \underline{X}_{2}, \ldots, \underline{X}_{n}$ follow iid $N_{p}(\underline{0}, \Sigma)$ then the $p \times p$ matrix $W=\sum_{i=1}^{n} \underline{X}_{i} \underline{X}_{i}{ }^{\prime}=X^{\prime} X$ has the distribution |  |  |  |  | c | $W \sim W_{p}(\underline{0}, \Sigma$ |
|  | a) $W \sim N_{p}(\underline{0}, \Sigma)$ | b) $W \sim N_{n}(\underline{0}, \Sigma)$ | c) $W \sim W_{p}(\underline{0}, \Sigma)$ |  | d) $W \sim W_{n}(\underline{0}, \Sigma)$ |  |  |
| 23 | The $\qquad$ distribution is a multivariate generalization of the chi-square distribution. |  |  |  |  | b | Hotelling' $\mathrm{s} T^{2}$ |
|  | a) <br> Multivariate Normal | b) <br> Hotelling's $T^{2}$ | c) Wishart distribution |  | d) all |  |  |
| 24 | If the element $c\{1,2\}$ of the covariance matrix $C$ is 114 , what is the value of $c\{2,1\}$ and what is the meaning? |  |  |  |  |  | 114, covarianc e |
|  | a)114, variance | b) 1/114, variance | c) 1/114, covariance |  | d) 114, covariance | d |  |
| 25 | This process is performed after extraction to obtain a more interpretable factor solution. |  |  |  |  | b | factor rotation |
|  | a) factor Normalization | b) factor rotation | c) factor optimization |  | d) factor interpretation |  |  |
| 26 | It is a correlation coefficient, which tells us the extent to which a question is measuring that factor. |  |  |  |  | d | factor loading |
|  | a) factor analysis | b) factor variable | c) factor rotation |  | d) factor loading |  |  |
| 27 | Testing the overall significance of multiple regression could be done by: |  |  |  |  | a | F-test |
|  | a) F-test b) | test | c) Chisquare test |  | Chow test |  |  |
| 28 | The smaller the standard errors, the stronger is the evidence that the estimates are statistically |  |  |  |  | b | significan <br> t |
|  | a) b) <br> insignific <br> ant  | ignificant | c) in conclusion |  | wrong |  |  |
| 29 | Find the linear model from the following: |  |  |  |  |  |  |


|  | $\begin{aligned} & \text { a) } Y= \\ & \beta_{0}+ \\ & e^{\beta_{1} X}+\epsilon \end{aligned}$ | b) $Y=\frac{\beta_{0}}{e^{\beta_{1} X}}+\epsilon$ | $\begin{aligned} & \text { c) } Y=\beta_{0}+ \\ & \log \left(\beta_{1} X\right)+\epsilon \end{aligned}$ | d) $Y=\beta_{0}+\beta_{1} X+\epsilon$ | d | $\begin{aligned} & Y \\ & =\beta_{0} \\ & +\beta_{1} X+\epsilon \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | For a Normal equation $X^{\prime} X \hat{\beta}=X^{\prime} Y$, the matrix $X^{\prime} X$ has a full rank. The solution of $\hat{\beta}$ has |  |  |  | a | a unique |
|  | a) a unique | b) an infinite | c) 0 | d) 2 times the rank of $X^{\prime} X$ |  |  |
| 31 | $100(1-\alpha) \%$ confidence interval of the slope $\beta_{1}$ in simple regression is given by |  |  |  | a | $\begin{aligned} & \hat{\beta}_{1} \\ & \pm t_{\frac{\alpha}{2}, n-2} S . E \end{aligned}$ |
|  | a) $\hat{\beta}_{1} \pm$ $t_{\frac{\alpha}{2}, n-2} S . E .$ | $\begin{aligned} & \text { b) } \hat{\beta}_{1} \pm \\ & t_{1-\frac{\alpha}{2}, n-2} S . E .\left(\hat{\beta}_{1}\right) \end{aligned}$ | $\begin{aligned} & \text { c) } \hat{\beta}_{1} \pm \\ & t_{\frac{\alpha}{2}, n-1} S . E .\left(\hat{\beta}_{1}\right) \end{aligned}$ | d) $\hat{\beta}_{1} \pm t_{\frac{\alpha}{2}, n} S . E .\left(\hat{\beta}_{1}\right)$ |  |  |
| 32 | Logistic regression is used for: |  |  |  | a | $\begin{gathered} \text { regressio } \\ \mathrm{n} \end{gathered}$ |
|  | a) regressio n | b) classification | c) clustering | d) all |  |  |
| 33 | The name of the link function for Poisson regression is: |  |  |  | C | log link |
|  | a) logistic link | b) identity link | c) log link | d) reciprocal link |  |  |
| 34 | The moving average (MA) process of order 1 is |  |  |  | a | $\begin{aligned} & Y_{t} \\ & =\emptyset Z_{t-1} \\ & +Z_{t} \end{aligned}$ |
|  | $\begin{aligned} & \text { a) } Y_{t}= \\ & \emptyset Z_{t-1}+ \\ & Z_{t} \end{aligned}$ | $\begin{aligned} & \text { b) } Y_{t}= \\ & Z_{t-1}+\emptyset Z_{t} \end{aligned}$ | $\begin{aligned} & \text { c) } Y_{t}= \\ & \emptyset Y_{t-1}+Z_{t} \end{aligned}$ | d) $Y_{t}=Y_{t-1}+\emptyset Z_{t}$ |  |  |
| 35 | A time series consists of |  |  |  | d | all |
|  | a) short term variations | b) long term variations | c) irregular variation | d) all |  |  |
| 36 | The increase in the number of patients in the hospital due to heat stroke is: |  |  |  | a | seasonal variation |
|  | a) <br> seasonal variation | b) secular trend | c) irregular variation | d) cyclical variation |  |  |


| 37 | For $\operatorname{AR}(1)$ model $Y_{t}=\varnothing Y_{t-1}+Z_{t}$, the random variable $Z_{t}$ follows: |  |  |  | b | $W N\left(0, \sigma^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a) iid $N\left(0, \sigma^{2}\right)$ | b) $W N\left(0, \sigma^{2}\right)$ | c) $N\left(0, \sigma^{2}\right)$ | d) independent $N\left(0, \sigma^{2}\right)$ |  |  |
| 38 | If the slope of the trend line $\hat{Y}_{t}=\hat{\beta}_{0}+\hat{\beta}_{1} t$ is positive, it shows |  |  |  | a | rising trend |
|  | a) rising trend | b) declining trend | c) stagnation | d) any of them |  |  |
| 39 | Previous probabilities in Bayes Theorem that are changed with the newly available information are called |  |  |  | d | posterior probabiliti es |
|  | a)independ ent probabilitie s | b)dependent probabilities | c) interior probabilities | d)posterior probabilities |  |  |
| 40 | The formula for Bayes theorem is |  |  |  | a | $\begin{aligned} & P(A \mid B) \\ & =\frac{P(B \mid A) P}{P(B)} \end{aligned}$ |
|  | $\begin{aligned} & \text { a) } P(A \mid B)= \\ & \frac{P(B \mid A) P(A)}{P(B)} \end{aligned}$ | $\begin{aligned} & \text { b) } P(A \mid B)= \\ & \frac{P(A)}{P(B)} \end{aligned}$ | $\begin{aligned} & \text { c) } P(A \mid B)= \\ & \frac{P(B \mid A)}{P(B)} \end{aligned}$ | d) $P(A \mid B)=\frac{1}{P(B)}$ |  |  |
| 41 | The method in which the previously calculated probabilities are revised with values of new probability is called |  |  |  | b | Bayes theorem |
|  | a) Revision theorem | b) Bayes theorem | C) <br> Dependent theorem | d) Updation theorem |  |  |
| 42 | Let $X_{1}, X_{2}, \ldots, X_{n}$ be the iid $B(\theta)$. Then conjugate prior distribution of $\theta$ is |  |  |  | C | Beta |
|  | a) <br> Student's t | b) Normal | c) Beta | d) Poisson |  |  |
| 43 | Which one is not the distribution of exponential family from the given distribution |  |  |  | d | Student-t |
|  | a) Poisson | b) Normal | c) Binomial | d) Student-t |  |  |

44 A family of parametric distribution in which mean is equal to

|  | variance is |  |  |  | d) | poisson <br> distribution |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a) Binomial distribution | b) Gamma distribution | c) Normal distribution | d) Poisson distribution |  |  |
| 45 | The distribution possessing the memoryless property is |  |  |  |  |  |
|  | a)gamma distribution | b)geometric distribution | c) <br> hypergeometric distribution | d) all the above | b) | geometric distribution |
| 46 | The distribution in which the probability at success draw varies is |  |  |  |  |  |
|  | a) hypergeometric distribution | b) geometric distribution | c) binomial distribution | d) discrete uniform distribution | a) | hypergeometric distribution |
| 47 | The distribution for which the mode does not exist is |  |  |  |  |  |
|  | a) normal distribution | b) t- <br> distribution | c) continuous <br> rectangular <br> distribution | d) F - <br> distribution | c) | continuous rectangular distribution |
| 48 | If $X \sim N\left(\mu, \sigma^{2}\right)$, the maximum probability at the point of inflexion of normal distribution is |  |  |  |  | $\mu \pm \sigma$ |
|  | a) $\pm \mu$ | b) $\mu \pm \sigma$ | c) $\sigma \pm \mu$ | d) $\pm \sigma$ | b) |  |
| 49 | An approximate relation between Q.D. and S.D. of normal distribution is |  |  |  |  | 3 Q.D. = 2 S.D. |
|  | a) 5 Q.D. $=4$ S.D. | $\begin{aligned} & \text { b) } 4 \text { Q.D. }=5 \\ & \text { S.D. } \end{aligned}$ | $\begin{aligned} & \text { c) } 2 \text { Q.D. }=3 \\ & \text { S.D. } \end{aligned}$ | $\begin{aligned} & \text { d) } 3 \text { Q.D. }=2 \\ & \text { S.D. } \end{aligned}$ | d) |  |
| 50 | The area under the standard normal curve beyond the lines $z= \pm 1.96$ is |  |  |  |  |  |
|  | a) 95 per cent | b) 90 per cent | c) 5 per cent | d) 10 per | c) | 5 per cent |


|  |  |  |  | cent |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | If the sample size $\mathrm{n}=2$, the student's t -distribution reduces to |  |  |  |  | Cauchy distribution |
|  | a) normal distribution | b) F- <br> distribution | c) Cauchy distribution | d) none of the above | c) |  |
| 52 | The relation between the mean and variance of $\chi^{2}$ with n d.f. is |  |  |  |  | $\begin{gathered} 2 \\ \text { mean=variance } \end{gathered}$ |
|  | a) mean=2 <br> b) 2 <br> variance <br> mean=varianc <br> e |  | c) mean $=$ variance | d) none of the above | b) |  |
| 53 | The distribution for which the moment generating function does not exist but moments exists is |  |  |  |  | all the above |
|  | a) Pareto distribution | b) t distribution | c) F-distribution | d) all the above | d) |  |
| 54 | In a multivariate study, the correlation between any two variable eliminating the effect of all other variables is called |  |  |  | c) | partial correlation |
|  | a) simple correlation | b)multiple correlation | c) partial correlation | d) partial regression |  |  |
| 55 | Parameters are those constants which occur in |  |  |  |  | probability <br> density <br> function |
|  | a) Samples | b) probability density function | c) a formula | d) none of the above | b) |  |
| 56 | Estimation of parameters in all scientific investigations is of |  |  |  |  | prime importance |
|  | a)prime importance | b) secondary importance | c) no use | d)deceptive nature | a) |  |
| 57 | Factorisation theorem for sufficiency is known as |  |  |  |  | Fisher-Neyman |
|  | a) Rao- | b) Crammer- | c) Chapman- | d)Fisher- | d) |  |


|  | Blackwell theorem | Rao theorem | Robin theorem | Neyman theorem |  | theorem |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 58 | Crammer-Rao inequality is based on |  |  |  |  | stringent conditions |
|  | a) stringent <br> conditions |  |  |  |  |  |
| 59 | The inequality for the lower bound of the variance of an estimator which is not based on stringent conditions was given by |  |  |  |  | Chapman- <br> Robins |
|  | a) Aitken and Silverstone | b)Neyman- <br> Pearson | c)Chapman- <br> Robins | d) none of the above | c) |  |
| 60 | Minimum Chi-square estimators are |  |  |  |  |  |
|  | a) consistent | b) asymptotically normal | c) efficient | d) all the above | d) | all the above |
| 61 | The maximum likelihood estimators are necessarily |  |  |  |  | sufficient |
|  | a) unbiased | b) sufficient | c) most efficient | d)unique | b) |  |
| 62 | A wrong decision about $H_{0}$ leads to |  |  |  |  | two kinds of error |
|  | a) one kind of error | b) two kinds of error | c)three kinds of error | d) four kinds of error | b) |  |
| 63 | Neyman-Pearson lemma provides |  |  |  |  |  |
|  | a) an unbiased test | b) a most powerful test | c)an admissible test | d) minimax test | b) | a most powerful test |
| 64 | The ratio of the likelihood function under $H_{0}$ and under the entire parametric space is called |  |  |  |  |  |


|  | a) probability ratio | b)sequential probability ratio | c) likelihood ratio | d) none of the above | c) | likelihood ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 65 | The degrees of freedom for statistic-t for paired t-test based on n pairs of observation is |  |  |  |  | n-1 |
|  | a) $2(n-1)$ | b) $\mathrm{n}-1$ | c) $2 \mathrm{n}-1$ | d) $\mathrm{n}-2$ | b) |  |
| 66 | Equality of several normal population means can be tested by |  |  |  |  | F-test |
|  | a) Bartlett's test | b) F-test | c) $\chi^{2}-t e s t$ | d) t-test | b) |  |
| 67 | In sequential probability test (SPRT) the sample size is |  |  |  |  | treatments <br> differ <br> significantly |
|  | a) treatments are equally effective | b)treatments <br> differ <br> significantly | c)no conclusion | d) none of the above | b) |  |
| 68 | Least square estimators of the parameters of linear model are |  |  |  |  | all the above |
|  | a) unbiased | b) BLUE | c) UMVU | d) all the above | d) |  |
| 69 | A uniformly most powerful test among the class of unbiased test is termed as |  |  |  |  | uniformly most powerful test |
|  | a) minimax test | b) minimax unbiased test | c) uniformly most powerful test | d) all the above | c) |  |
| 70 | SPRT was initiated by |  |  |  |  | A. Wald |
|  | a) R. A. Fisher | b)A. Wald | c)G. W. <br> Snedecor | d)Thomas <br> Bayes | b) |  |
| 71 | A contingency table having a zero count is called |  |  |  |  |  |




|  | a)W.G. <br> Cochran | b) M.H. Hansen | c) D.B. Lahiri | d) P.C. <br> Mahalonobis | c) | D.B. Lahiri |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 82 | Which of the following sampling designs will be categorised as non-probability sampling |  |  |  |  | all the above |
|  | a) haphazard sampling | b) convenience sampling | c) judgement sampling | d)all the above | d) |  |
| 83 | There are more chance of non-sampling errors than sampling errors in case of |  |  |  | d) | all the above |
|  | a) studies of large sample | b) complete enumeration | c) insufficient investigation | d) all the above |  |  |
| 84 | Which one of the following is an example of random process in communication? |  |  |  | c) | Both a) and b) |
|  | a) Channel noise | b) Interference | c) Both a) and <br> b) | d) None of the above |  |  |
| 85 | The random walk is an example of |  |  |  | a) | Nondeterministic process |
|  | a) Non- <br> deterministic <br> process | b) Deterministic process | c) Both a and b | d) None of the above |  |  |
| 86 | Stochastic process are |  |  |  | c) | Random in nature and are a function of time |
|  | a) Random in nature | b) Are function of time | c) Random in nature and are a function of time | d) None of the above |  |  |
| 87 | In post-independence India, the registration of Births and Deaths Act was passed in |  |  |  |  |  |


|  | a) 1948 | b)1959 | c)1969 | d)1979 | c) | 1969 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88 | The fertility of a women in India is maximum in the age group |  |  |  |  | 25-29 |
|  | a)15-20 | b) 20-24 | c) 25-29 | d)15-29 | c) |  |
| 89 | The age-specific death rate for the babies of age less than one year is specifically called |  |  |  | b) | infant mortality rate |
|  | a)neonatal b)infant <br> death rate mortality rate |  | c) maternal mortality rate | d)foetal death rate |  |  |
| 90 | A life table based on the experience of actual cohort is called |  |  |  |  | both a) and b) |
|  | a) generation life table | b) fluent life table | c) both a) and b) | d) neither <br> a) nor b) | C) |  |
| 91 | Chance variation is respect of quality control of a product is |  |  |  | d) | all the above |
|  | a) tolerable | b) not <br> effecting the quality of a product | c) uncontrollable | d)all the above |  |  |
| 92 | The cause leading to vast variation in the specification of a product are usually due to |  |  |  |  | assignable <br> causes |
|  | a) random process | b) assignable causes | c) non-traceable causes | d) all the above | b) |  |
| 93 | R-charts are preferable over $\sigma$-charts because |  |  |  |  |  |
|  | a) $R$ and S.D. <br> fluctuate together in case of small samples | b) R can be easily calculated | c) R-charts are economical | d) all the above | d) | all the above |
| 94 | The graph of the proportion of defectives in the lot against |  |  |  |  |  |



|  | Pearson | Galton | Bacon |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 100 | The branch of biostatistics that deals with methods of collection, <br> organization and presentation of data is called as |  |  |  |
| a) inferential <br> biostatistics b) descriptive <br> biostatistics c) both a) and <br> b) d) comparative <br> biostatistics b) | descriptive <br> biostatistics |  |  |  |

## SPACE FOR ROUGH WORK

