

Springer Proceedings in Physics 265

Soumitra Sengupta ·  
Samrat Dey · Saurya Das ·  
Dhruba J. Saikia · Sudhakar Panda ·  
Ramakrishna Podila *Editors*

# Selected Progresses in Modern Physics

Proceedings of TiMP 2021

 Springer

# **Springer Proceedings in Physics**

Volume 265

Indexed by Scopus

The series Springer Proceedings in Physics, founded in 1984, is devoted to timely reports of state-of-the-art developments in physics and related sciences. Typically based on material presented at conferences, workshops and similar scientific meetings, volumes published in this series will constitute a comprehensive up-to-date source of reference on a field or subfield of relevance in contemporary physics. Proposals must include the following:

- name, place and date of the scientific meeting
- a link to the committees (local organization, international advisors etc.)
- scientific description of the meeting
- list of invited/plenary speakers
- an estimate of the planned proceedings book parameters (number of pages/articles, requested number of bulk copies, submission deadline).

***Please contact:***

For Americas and Europe: Dr. Zachary Evenson; [zachary.evenson@springer.com](mailto:zachary.evenson@springer.com)

For Asia, Australia and New Zealand: Dr. Loyola DSilva; [loyola.dsilva@springer.com](mailto:loyola.dsilva@springer.com)

More information about this series at <https://link.springer.com/bookseries/361>

Soumitra Sengupta · Samrat Dey · Saurya Das ·  
Dhruba J. Saikia · Sudhakar Panda ·  
Ramakrishna Podila  
Editors

# Selected Progresses in Modern Physics

Proceedings of TiMP 2021

 Springer

*Editors*

Soumitra Sengupta  
Indian Association for the Cultivation  
of Science  
Kolkata, India

Saurya Das  
University of Lethbridge  
Lethbridge, AB, Canada

Sudhakar Panda  
National Institute of Science Education  
and Research  
Bhubaneswar, Odisha, India

Samrat Dey  
Pragjyotish College  
Guwahati, Assam, India

Dhruba J. Saikia  
University Centre for Astronomy  
and Astrophysics  
Pune, Maharashtra, India

Ramakrishna Podila  
Clemson University  
Clemson, SC, USA

ISSN 0930-8989

ISSN 1867-4941 (electronic)

Springer Proceedings in Physics

ISBN 978-981-16-5140-3

ISBN 978-981-16-5141-0 (eBook)

<https://doi.org/10.1007/978-981-16-5141-0>

© The Editor(s) (if applicable) and The Author(s), under exclusive license to Springer Nature Singapore Pte Ltd. 2021

This work is subject to copyright. All rights are solely and exclusively licensed by the Publisher, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilms or in any other physical way, and transmission or information storage and retrieval, electronic adaptation, computer software, or by similar or dissimilar methodology now known or hereafter developed.

The use of general descriptive names, registered names, trademarks, service marks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

The publisher, the authors and the editors are safe to assume that the advice and information in this book are believed to be true and accurate at the date of publication. Neither the publisher nor the authors or the editors give a warranty, expressed or implied, with respect to the material contained herein or for any errors or omissions that may have been made. The publisher remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

This Springer imprint is published by the registered company Springer Nature Singapore Pte Ltd. The registered company address is: 152 Beach Road, #21-01/04 Gateway East, Singapore 189721, Singapore

# Preface

The Springer International Conference on Trends in Modern Physics (TiMP) 2021, the third annual conference of the Physics Department of Assam Don Bosco University (ADBU), was organised from 26 to 27 February, 2021, by the department, in collaboration with Indian Association of Physics Teachers, after successfully organising TiMP 2019 and TiMP 2020. A large number of participants, from various universities, colleges and institutes of India and abroad, presented around hundred research papers in the event. Due to the restrictions imposed by the COVID-19 pandemic, the conference was held in hybrid mode, with half of the participants making their presentations online and the remaining half presenting offline, in person. The organisers of the conference made all possible efforts to ensure that every delegate is able to seamlessly access all the presentations, irrespective of whether the presenter or the presentation is online or offline. To this end, all the offline presentations were also streamed live via web-conferencing and all the posters were made available online. Selected papers of TiMP 2021 have found their place in the proceedings after going through the due processes of peer reviews.

It was a felt need by the department to hold yearly national conferences on TiMP, as in this region there were no such yearly conferences of physics, where young researchers can share their ideas and get suggestions and help from renowned academicians of the country and other parts of the world. It may be noted, in this context, that the Physics Department, ADBU, ever since its inception in 2018, has been working at different levels to popularise elementary as well as advanced physics through various other approaches, like symposiums, workshops, refresher course, etc. The TiMP conference series has not been confined to any specific branch of physics, but, practically, to all the major disciplines of physics with the following underlying philosophy. While it is true that each discipline of physics has become so highly specialised that it is not easily legible to a person of another discipline, we must remember that over the history of the development of modern science, physicists' contributions were not only across different branches of physics but also to various other fields of science. For example, Marie Curie, a physicist, won a Nobel Prize in chemistry, apart from a Nobel Prize in physics. James Watson who got the Nobel Prize for proposing the double helix structure of the DNA molecule was actually

inspired by physics Nobel Laureate Erwin Schrödinger's book, "What Is Life?". World Wide Web (WWW) was invented in a physics research institute, CERN. The first computer simulation was developed in nuclear physics. Physicists' contribution to mathematics can be exemplified by the development of calculus by Isaac Newton. Venki Ramakrishnan, a Ph.D. in physics, got the Nobel Prize for his studies of the structure and function of the ribosome which is important in the production of antibiotics. The list of physicists contributing to other fields of science is actually too long. Thus, it is evident that if people from physics can make so many contributions to additional domains of science outside the realm of physics, it is both productive and likely for them, even if they are from specific branches of physics, to contribute to and collaborate with other disciplines within physics. With that philosophy in mind, this multidisciplinary physics conference series was conceptualised and has been being implemented successfully.

We thank the convener of the international conference, Mr. Parag Bhattacharya, together with the co-conveners, Dr. Debajyoti Dutta and Dr. Ngangom Aomoa. We also express our gratitude to all the reviewers, Dr. Lalthakimi Zadeng, Dr. Yubaraj Sharma, Dr. Simanta Chutia, Prof. Sunandan Baruah, Dr. Sumita Kumari Sharma, Dr. Kaustubh Bhattacharyya, Dr. Shantu Saikia, Dr. Debajyoti Dutta, Dr. Ngangom Aomoa, Prof. Atri Deshamukhya, Dr. Subhankar Roy, Dr. Debasish Borah, Dr. Wandahun Longtraï Reenbohn, Dr. Rashi Borgohain, Prof. Pritam Deb, Dr. Pralay Kumar Karmakar, Dr. Ashok Kumar Jha, Dr. Umananda Dev Goswami, Dr. Hemen Kumar Kalita and Dr. Subhaditya Bhattacharya. Finally, we thank all the authors for their contributions in the proceedings.

Kolkata, India

Guwahati, India

Lethbridge, Canada

Pune, India

Bhubaneswar, India

Clemson, USA

Soumitra Sengupta

Samrat Dey

Saurya Das

Dhruba J. Saikia

Sudhakar Panda

Ramakrishna Podila

# Contents

<b>1</b>	<b>A Comparative Study of Experimental and Theoretical <math>Z</math> (Compressibility Factor) of Argon as a Typical Representative of Simple Fluids</b> .....	<b>1</b>
	Yatendra S. Jain and Simanta Chutia	
<b>2</b>	<b>A Theoretical Review to Analyze the Response Between the Radiographic Film and the Living Tissue in Terms of Energy Absorption</b> .....	<b>9</b>
	Dipankar Bhagabati, Rangaraj Bhattacharjee, Biswajit Nath, Kalyanjit Dutta Baruah, and B. K. Duara	
<b>3</b>	<b>Biosynthesis, Characterization and Antibacterial Performance of Trimanganese Tetraoxide Nanoparticles Using <i>Azadirachta Indica</i> Leaf Extract</b> .....	<b>17</b>
	S. Jessie Jancy Rani, A. S. I. Joy Sinthiya, and G. Jeeva Rani Thangam	
<b>4</b>	<b>Calculating CP Invariance Using Weak Basis Invariants in Hybrid Textures of Neutrino Mass Matrix</b> .....	<b>31</b>
	Madan Singh	
<b>5</b>	<b>Characteristic Range of <math>^{238}\text{U}</math> Ion in Polycarbonates</b> .....	<b>43</b>
	J. P. Gewali and M. Singh	
<b>6</b>	<b>Comparison of Protein Interaction with Different Shaped PbS Nanoparticles and Corona Formation</b> .....	<b>51</b>
	A. K. Mishra, A. K. Bhunia, and S. Saha	
<b>7</b>	<b>Dark Matter in Singlet Scalar, Inert Doublet and Mixed Scalar Dark Matter Models</b> .....	<b>65</b>
	Nilavjyoti Hazarika and Kalpana Bora	
<b>8</b>	<b>Dependence of Particle Current and Diffusion on the System Parameters in a Model Under-damped Inhomogeneous Periodic Potential System</b> .....	<b>73</b>
	Francis Iawphniaw, Samrat Dey, and Shantu Saikia	



<b>9</b>	<b>Development of Agro-waste Based Nanosized Cellulose</b> .....	<b>85</b>
	Suvangshu Dutta	
<b>10</b>	<b>Distribution of X-Ray Flux: RXTE-PCA Observation of Cygnus X-1</b> .....	<b>95</b>
	Kabita Deka, Zahir Shah, Ranjeev Misra, and Gazi Ameen Ahmed	
<b>11</b>	<b>Establishing a Mathematical and Radiological Relation Between the Malignant Tumour Inside the Body and the Outer Body Surface of the Patient</b> .....	<b>103</b>
	Kuldeep Sharma, Ananya Bhattacharjee, Rangaraj Bhattacharjee, Biswajit Nath, Kalyanjit Dutta Baruah, and Dipankar Bhagabati	
<b>12</b>	<b>Exploring Invisible Neutrino Decay at Long-Baseline Experiments</b> .....	<b>115</b>
	Zannatun Firdowzy Dey and Debajyoti Dutta	
<b>13</b>	<b>Flux Distribution Study of Mkn 421 with SPOL, RXTE and Fermi-LAT Telescopes</b> .....	<b>125</b>
	Rukaiya Khatoon, Zahir Shah, Raj Prince, Ranjeev Misra, and Rupjyoti Gogoi	
<b>14</b>	<b>Growth, Structural, Optical, Thermal and Mechanical Studies of a Novel Nickel Sulphate Admixed Sulphamic Acid Single Crystals for Optical Applications</b> .....	<b>135</b>
	S. Anciya, A. S. I. Joy Sinthiya, P. Selvarajan, and R. Sree Devi	
<b>15</b>	<b>Impact of Multi-Nucleon Effects on Neutrino Scattering Cross Section and Events at Near and Far Detectors of NO<math>\nu</math>A Experiment</b> .....	<b>147</b>
	Paramita Deka and Kalpana Bora	
<b>16</b>	<b>Impact of Texture Zeros of Neutrino Mass Matrix on Dark Matter Phenomenology</b> .....	<b>153</b>
	Nayana Gautam and Mrinal Kumar Das	
<b>17</b>	<b>Improved Potential Approach and Masses of Heavy Flavour Mesons</b> .....	<b>159</b>
	Dhanjit Talukdar and Jugal Lahkar	
<b>18</b>	<b><i>keV</i> Sterile Neutrino Mass Model and Related Phenomenology</b> ....	<b>167</b>
	Pritam Das and Mrinal Kumar Das	
<b>19</b>	<b>Lee-Wave Clouds in Martian Atmosphere: A Study Based on the Images Captured by Mars Color Camera (MCC)</b> .....	<b>173</b>
	Jyotirmoy Kalita, Manoj Kumar Mishra, and Anirban Guha	
<b>20</b>	<b>Microscopic Foundation of Some Empirical Rules and <math>Z(P_r)</math> of a Simple Fluid</b> .....	<b>193</b>
	Yatendra S. Jain	

<b>21</b>	<b>Moisture Content Study of Soil Found in Sung Valley, Meghalaya</b> .....	211
	Jodie T. Rynngnga and B. M. Jyrwa	
<b>22</b>	<b>Neutrinoless Double Beta Decay in a Flavor Symmetric Scotogenic Model</b> .....	217
	Lavina Sarma, Bichitra Bijay Boruah, and Mrinal Kumar Das	
<b>23</b>	<b>Novel Design of Multi-Band Double U Slotted Microstrip Patch Antenna with DGS for Satellite and Radar Applications</b> ....	223
	P. Arockia Michael Mercy and K. S. Joseph Wilson	
<b>24</b>	<b>Observation and Characterization of Cyclic Particle Growth Process in rf Discharge of Ar-C<sub>2</sub>H<sub>2</sub> Gas Mixture</b> .....	235
	Bidyut Chutia, S. K. Sharma, and H. Bailung	
<b>25</b>	<b>Optical Study of Liquid Dispersed Few-Layered WS<sub>2</sub> Nanosheets</b> .....	243
	Ashamoni Neog and Rajib Biswas	
<b>26</b>	<b>Our Universe: The Known, Unknown, and Some Speculations</b> .....	251
	Saurya Das	
<b>27</b>	<b>Phenomenological Study of Neutrino Mass Matrices with One Vanishing Minor and Zero Sum of Mass Eigenvalues with Majorana Phases</b> .....	257
	Sangeeta Dey and Mahadev Patgiri	
<b>28</b>	<b>Programmable Electro-Mechanical Dust Dispenser for Dusty Plasma Experimental Device</b> .....	265
	Nipan Das, S. S. Kausik, and B. K. Saikia	
<b>29</b>	<b>Radiation Exposure Due to Indoor Radon and Thoron in the Environs of Jowai Town, Meghalaya, India</b> .....	277
	A. Pyngrope and A. Saxena	
<b>30</b>	<b>Realization of Left-Right Symmetric Model by Discrete Flavor Symmetries</b> .....	285
	Bichitra Bijay Boruah and Mrinal Kumar Das	
<b>31</b>	<b>Relation Between the Variability of the Kilo-Hertz Quasi-Periodic Oscillations and the Low-Frequency Noise in 4U1608–52</b> .....	293
	Soma Mandal	
<b>32</b>	<b>Review on Magnetism in Nanomaterials and Superparamagnetism</b> .....	303
	Bandana Gogoi and Upamanyu Das	

<b>33</b>	<b>Role of Laser Pre-pulse and Target Density Modification on the Acceleration of Protons from a Hydrogen Plasma Sphere</b> ...	<b>313</b>
	Ankita Bhagawati	
<b>34</b>	<b>Searching the Limits on Heavy Majorana Mass Spectrum for Different Textures of Majorana Mass Matrices</b> .....	<b>321</b>
	Maibam Ricky Devi and Kalpana Bora	
<b>35</b>	<b>Smartphone-Based Colorimetric Analyzer for Detection of Phosphate in Water</b> .....	<b>327</b>
	Priyanka Das, Biprav Chetry, and Pabitra Nath	
<b>36</b>	<b>Structural, Morphological and Optical Properties of Titanium Dioxide Nanomaterials Prepared by Sol Gel Technique</b> .....	<b>337</b>
	Ansh Gupta, Deepak Kumar, Anupam Kumar, Jeeban P. Gewali, and Ankush Thakur	
<b>37</b>	<b>Structural, Spectral and Optical Properties of Lithium Sulphate Monohydrate L-Valine Semiorganic Crystal</b> .....	<b>347</b>
	Chandrashekhar M. Bhambere and N. G. Durge	
<b>38</b>	<b>Study of Ion-Acoustic Waves in Two-Electron Temperature Plasma</b> .....	<b>355</b>
	G. Sharma, K. Deka, R. Paul, S. Adhikari, R. Moulick, S. S. Kausik, and B. K. Saikia	
<b>39</b>	<b>Study of Plasma Sheath in the Presence of Dust Particles in an Inhomogeneous Magnetic Field</b> .....	<b>363</b>
	K. Deka, R. Paul, G. Sharma, S. Adhikari, R. Moulick, S. S. Kausik, and B. K. Saikia	
<b>40</b>	<b>Study of Radiation Interactions in Makrofol-E and LR-115 Detectors Using SSNTD Technique</b> .....	<b>375</b>
	J. P. Gewali, P. Sheron, A. Thakur, and B. Jaishy	
<b>41</b>	<b>Study of Structural, Electrical and Magnetic Properties of Nd-Ti Co-Doped BiFeO<sub>3</sub> Nanoparticles</b> .....	<b>387</b>
	Sanjay Godara	
<b>42</b>	<b>Frictional Effect of Neutrals Hall Current and Radiative Heat-Loss Functions on Thermal Instability of Two-Component Plasma</b> .....	<b>395</b>
	Sachin Kaothekar	

<b>43</b>	<b>Transport Coefficients of Dense Stellar Plasma in Strong Magnetic Field</b> .....	<b>411</b>
	Soma Mandal	
<b>44</b>	<b>Variation of High and Low Energetic Electron Densities Across a Magnetic Filter in a Hot Cathode Discharge</b> .....	<b>423</b>
	Jocelyn Sangma and Monojit Chakraborty	

# Contributors

**S. Adhikari** Department of Physics, University of Oslo, Oslo, Norway

**Gazi Ameen Ahmed** Department of Physics, Tezpur University, Napaam, Assam, India

**S. Anciya** PG and Research Department of Physics, The M. D. T. Hindu College, Tirunelveli, Tamil Nadu, India;  
Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli-12, Tamil Nadu, India

**H. Bailung** Dusty Plasma Laboratory, Physical Sciences Division, Institute of Advanced Study in Science and Technology (IASST), Guwahati, Assam, India

**Kalyanjit Dutta Baruah** State Cancer Institute, Gauhati Medical College, Guwahati, Assam, India

**Dipankar Bhagabati** State Cancer Institute, Gauhati Medical College, Guwahati, Assam, India

**Ankita Bhagawati** Department of Physics, Tezpur University, Tezpur, Assam, India

**Chandrashekhar M. Bhambere** Department of Physics, S. S. and L. S. Patkar-Varde College, Mumbai, Maharashtra, India

**Ananya Bhattacharjee** Department of Mathematics, Assam University Silchar, Silchar, Assam, India

**Rangaraj Bhattacharjee** State Cancer Institute, Gauhati Medical College, Guwahati, Assam, India

**A. K. Bhunia** Department of Physics, Government General Degree College at Gopiballavpur-II, Jhargram, Beliaberah, West Bengal, India

**Rajib Biswas** Applied Optics and Photonics Lab, Department Of Physics, Tezpur University, Tezpur, Assam, India

**Kalpna Bora** Physics Department, Gauhati University, Guwahati, Assam, India

**Bichitra Bijay Boruah** Tezpur University, Tezpur, Assam, India

**Monojit Chakraborty** Centre of Plasma Physics-Institute for Plasma Research, Tepesia Sonapur, Assam, Kamrup (M), India

**Biprav Chetry** Applied Photonics & Nano-Photonics Laboratory, Department of Physics, Tezpur University, Tezpur, Assam, India

**Bidyut Chutia** Dusty Plasma Laboratory, Physical Sciences Division, Institute of Advanced Study in Science and Technology (IASST), Guwahati, Assam, India

**Simanta Chutia** Department of Physics, St. Anthony's College, Shillong, India

**Mrinal Kumar Das** Department of Physics, Tezpur University, Tezpur, India; Department of Physics, Tezpur University, Napaam, Assam, India

**Nipan Das** Centre of Plasma Physics-Institute for Research, Sonapur, Assam, India

**Pritam Das** Department of Physics, Tezpur University, Napaam, Assam, India

**Priyanka Das** Applied Photonics & Nano-Photonics Laboratory, Department of Physics, Tezpur University, Tezpur, Assam, India

**Saurya Das** Theoretical Physics Group, Department of Physics and Astronomy and Quantum Alberta, University of Lethbridge, Lethbridge, AB, Canada

**Upamanyu Das** Rajiv Gandhi University, Doimukh, A.P, India

**K. Deka** Centre of Plasma Physics, Institute for Plasma Research, Sonapur, Kamrup(M), Assam, India

**Kabita Deka** Department of Physics, Tezpur University, Napaam, Assam, India

**Paramita Deka** Department of Physics, Gauhati University, Guwahati, Assam, India

**Maibam Ricky Devi** Department of Physics, Gauhati University, Guwahati, Assam, India

**Samrat Dey** Department of Physics, Assam Don Bosco University, Guwahati, Assam, India

**Sangeeta Dey** Cotton University, Guwahati, India

**Zannatun Firdowzy Dey** Department of Physics, Assam Don Bosco University, Sonapur, India

**B. K. Duara** Department of Radiology, Gauhati Medical College & Hospital, Guwahati, Assam, India

**N. G. Durge** Department of Physics, S. S. and L. S. Patkar-Varde College, Mumbai, Maharashtra, India

**Debajyoti Dutta** Department of Physics, Assam Don Bosco University, Sonapur, India

**Suvangshu Dutta** Dept. of Chemistry, D.R. College, Golaghat, Assam, India

**Nayana Gautam** Department of Physics, Tezpur University, Tezpur, India

**J. P. Gewali** Department of Physics, Lovely Professional University, Jalandhar, Punjab, India;

Department of Physics, Lovely Professional University, Phagwara, Punjab, India

**Jeeban P. Gewali** Department of Physics, School of Chemical Engineering and Physical Sciences, Lovely Professional University, Phagwara, Punjab, India

**Sanjay Godara** Department of Physics, MLV Government College, Bhilwara, Rajasthan, India

**Bandana Gogoi** Rajiv Gandhi University, Doimukh, A.P, India

**Rupjyoti Gogoi** Tezpur University, Napaam, Assam, India

**Anirban Guha** Department of Physics, Tripura University, Suryamaninagar, Tripura, India

**Ansh Gupta** Department of Physics, School of Chemical Engineering and Physical Sciences, Lovely Professional University, Phagwara, Punjab, India

**Nilavjyoti Hazarika** Physics Department, Gauhati University, Guwahati, Assam, India

**Francis Iawphniaw** Department of Physics, St. Anthony's College, Shillong, India; Department of Physics, Assam Don Bosco University, Guwahati, Assam, India

**Yatendra S. Jain** Department of Physics, North-Eastern Hill University, Shillong, India

**B. Jaishy** Department of Physics, Lovely Professional University, Phagwara, Punjab, India

**B. M. Jyrwa** Department of Physics, North Eastern Hill University, Umshing, Shillong, India

**Jyotirmoy Kalita** Department of Physics, Tripura University, Suryamaninagar, Tripura, India

**Sachin Kaotekar** Department of Physics, Mahakal Institute of Technology & Management, Ujjain, M.P, India

**S. S. Kausik** Centre of Plasma Physics, Institute for Plasma Research, Sonapur, Kamrup(M), Assam, India

**Rukaiya Khatoon** Tezpur University, Napaam, Assam, India

**Anupam Kumar** Department of Biotechnology, School of Bioengineering and Biosciences, Lovely Professional University, Phagwara, Punjab, India

**Deepak Kumar** Department of Chemistry, School of Chemical Engineering and Physical Sciences, Lovely Professional University, Phagwara, Punjab, India

**Jugal Lahkar** Department of Physics, Pragjyotish College, Guwahati, India

**Soma Mandal** Department of Physics, Government Girls' General Degree College, Kolkata, India

**P. Arockia Michael Mercy** PG & Research Department of Physics, Arul Anandar College, Karumathur, Madurai, India

**A. K. Mishra** Department of Physics, Vidyasagar University, Paschim Medinipur, Midnapore, West Bengal, India

**Manoj Kumar Mishra** Space Applications Centre, Indian Space Research Organization, Ahmedabad, India

**Ranjeev Misra** Inter-University Center for Astronomy and Astrophysics, Pune, India;

Inter-University Center for Astronomy and Astrophysics, Ganeshkhind Pune, India

**R. Moulick** Department of Physics, Rangapara College, Rangapara, Sonitpur, Assam, India

**Biswajit Nath** Silchar Medical College Hospital, Silchar, Assam, India

**Pabitra Nath** Applied Photonics & Nano-Photonics Laboratory, Department of Physics, Tezpur University, Tezpur, Assam, India

**Ashamoni Neog** Applied Optics and Photonics Lab, Department Of Physics, Tezpur University, Tezpur, Assam, India

**Mahadev Patgiri** Cotton University, Guwahati, India

**R. Paul** Centre of Plasma Physics, Institute for Plasma Research, Sonapur, Kamrup(M), Assam, India

**Raj Prince** Center for Theoretical Physics, Polish Academy of Sciences, Warsaw, Poland

**A. Pyngrope** Department of Physics, North-Eastern Hill University, Shillong, India

**S. Jessie Jancy Rani** PG and Research Department of Physics, The M.D.T. Hindu College, Tirunelveli, Tamil Nadu, India;  
Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli-12, Tamil Nadu, India

**Jodie T. Ryngnga** Department of Physics, North Eastern Hill University, Umshing, Shillong, India

**S. Saha** Department of Physics, Vidyasagar University, Paschim Medinipur, Midnapore, West Bengal, India



**B. K. Saikia** Centre of Plasma Physics, Institute for Plasma Research, Sonapur, Kamrup(M), Assam, India

**Shantu Saikia** Department of Physics, St.Anthony's College, Shillong, India

**Jocelyn Sangma** Centre of Plasma Physics-Institute for Plasma Research, Tepesia Sonapur, Assam, Kamrup (M), India

**Lavina Sarma** Tezpur University, Tezpur, Assam, India

**A. Saxena** Department of Physics, North-Eastern Hill University, Shillong, India

**P. Selvarajan** Department of Physics, Aditanar College of Arts and Science, Tiruchendur, Tamil Nadu, India;  
Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli-12, Tamil Nadu, India

**Zahir Shah** Inter-University Center for Astronomy and Astrophysics, Pune, India;  
Inter-University Center for Astronomy and Astrophysics, Ganeshkhind Pune, India

**G. Sharma** Centre of Plasma Physics, Institute for Plasma Research, Sonapur, Kamrup(M), Assam, India

**Kuldeep Sharma** State Cancer Institute, Gauhati Medical College, Guwahati, Assam, India

**S. K. Sharma** Dusty Plasma Laboratory, Physical Sciences Division, Institute of Advanced Study in Science and Technology (IASST), Guwahati, Assam, India

**P. Sheron** Department of Physics, Lovely Professional University, Phagwara, Punjab, India

**M. Singh** Department of Physics, Lovely Professional University, Jalandhar, Punjab, India

**Madan Singh** Department of Physics, M.N.S. Government College Bhiwani, Haryana, India

**A. S. I. Joy Sinthiya** PG and Research Department of Physics, The M.D.T. Hindu College, Tirunelveli, Tamil Nadu, India

**R. Sree Devi** Department of Physics, Aditanar College of Arts and Science, Tiruchendur, Tamil Nadu, India;  
Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli-12, Tamil Nadu, India

**Dhanjit Talukdar** Department of Physics, Pragjyotish College, Guwahati, India

**A. Thakur** Department of Physics, Lovely Professional University, Phagwara, Punjab, India

**Ankush Thakur** Department of Physics, School of Chemical Engineering and Physical Sciences, Lovely Professional University, Phagwara, Punjab, 144411 India

**G. Jeeva Rani Thangam** PG and Research Department of Physics, Pope's College, Thoothukudi, Tamil Nadu, India

**K. S. Joseph Wilson** PG & Research Department of Physics, Arul Anandar College, Karumathur, Madurai, India

# Chapter 32

## Review on Magnetism in Nanomaterials and Superparamagnetism



Bandana Gogoi and Upamanyu Das

**Abstract** Nanotechnology plays a prominent role in the fabrication of novel materials by controlling the structure of matter at the nanometric scale changing properties at a molecular level. The particles with nanodimensions change their material properties in a dramatic way showing uniqueness in behaviour with modified properties. In many ferromagnetic materials when the size is reduced to the nanoscale level, the magnetic properties enhance in a unique way, thus leading to a superparamagnetic state. The magnetic moment of the material randomly flips the direction of their magnetization, and the random orientations of magnetic spins inside the particles result in zero remanent magnetization and zero coercivity. An unusual change in the hysteresis loop shows the magnetization curve passing through the origin, showing the state of zero magnetization.

### 32.1 Introduction

At the nanoscopic dimension, the magnetic behaviours of magnetic nanomaterial show significant differences from those observed at bulk scale with the same chemical composition [1–3]. As the size is reduced material property gradually moves from the regime of bulk material behaviour to molecular-level material behaviour. Drastic changes in properties took place at the molecular level.

With the reduction of size, the basic magnetic properties or magnetism connected to different bulk ferro and anti-ferromagnetic material changes to develop in different modified ways. These changes may be shown to occur from the dimension of the material which becomes comparable to some of the basic fundamental characteristic lengths of one or more of various physical properties that are more relevant to the magnetic properties (e.g. the size of magnetic domains, exchange length etc.). With reduced size to nanoscale level, translation symmetry of the magnetic material breaks giving rise to specific sites with reduced coordination numbers, broken exchange and a higher proportion of atoms on the surface increasing surface effect. A high surface

---

B. Gogoi (✉) · U. Das  
Rajiv Gandhi University, Doimukh, A.P, India

to volume ratio brings more close contact with the exterior system. The spin-wave spectrum of the nanometric material also tends to change and this change can be observed as spin-wave energy becomes comparable to the thermal energy which plays a prominent role in developing new magnetic properties [3–12].

Nanoscale magnetism has been basically studied to be developing from unpaired d-orbital electrons as well as the coupling effect of these electrons with nuclear spins. At nanosized dimension, the surface area gets more exposure to the exterior neighbouring system, as a result of which the material achieves higher modified functionalities like increased reactivity, higher catalytic action and decreased melting point due to surface effect. The surface energy increases with increased surface area and hence surface effect dominates over the other observed effects at nanosized dimension. This increased surface energy effect also helps in developing extraordinary magnetic behaviours in magnetic nanomaterials. Particle size plays a significant role in determining the basic material property of any material like magnetic, electrical, optical or electronic property. Therefore increasing interest has been developed to study magnetic nanomaterials in recent times due to their size-dependent properties [13, 14].

Figure 32.1 shows the typical hysteresis loop of any bulk ferromagnetic material. In order to observe the changes of magnetic properties of ferro or anti-ferromagnetic materials with particle size, the magnetic hysteresis curve of normal bulk ferromagnetic material needs to be understood. In normal ferromagnetic behaviour, the curve is observed to have a remanence and a coercive field, i.e. the line of magnetization curve does not pass through zero or origin.

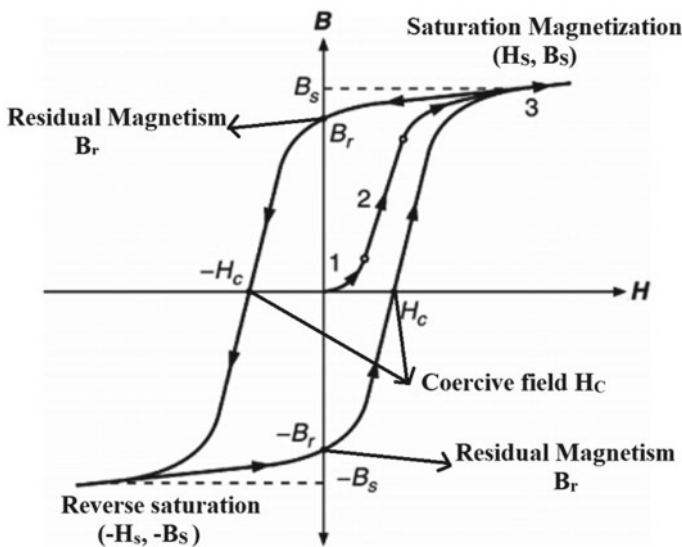


Fig. 32.1 Magnetization curve of ferromagnetic material in a bulk state

The development of uniqueness in the magnetic property of magnetic materials can be studied to be originated from the division of magnetic material into distinct and well-separated magnetic domains with magnetic moment alignment. The change in magnetic moment directions in magnetic domains may correspond to the total cancellation of the magnetic moment or may tend to minimize the total average magnetization to become nearly zero.

There are various interaction terms in a magnetic system that contribute to the total internal energy of a magnetic material and can be expressed as

$$E_{tot} = E_{ex} + E_A + E_{ms} + E_{ext} \quad (32.1)$$

**Exchange interaction ( $E_{ex}$ )** is responsible for the establishment of magnetic order in magnetic materials. This interaction arises from a quantum effect due to the indistinguishability of the electron.

$H = -2JS_iS_j$  where  $J$  is the exchange constant.  $S_i$  and  $S_j$  are spins.

**Magnetostatic energy ( $E_{ms}$ )** or dipolar energy is the measure of the magnetic energy of a magnetic sample because of its own magnetic field. This field is the demagnetizing field that arises from the divergence of magnetization.

**Magnetic anisotropy ( $E_A$ )** is crystallogenic in origin. The shape of the sample, the stress in the material and atomic segregation determine the value of magnetic anisotropy energy. The energy of a magnetically ordered sample depends on the relative direction of the magnetization and the structural axes; for example, a solid has an axis along which the energy is at a minimum. The anisotropy energy  $E_A$  is written as a function of the direction cosines  $\alpha_1, \alpha_2$  and  $\alpha_3$  defined in relation to the axes of the crystal.

**Uniaxial anisotropy** is the approximation that in some samples anisotropy depends only on the angle  $\theta$  between the magnetization and a given axis. The anisotropy energy per unit volume takes the form

$$E_A/V = K_1 \sin^2 \theta + K_2 \sin^4 \theta \quad (32.2)$$

where  $\theta$  is the angle of magnetization with the single axis, and depending on the magnitude of anisotropy constants  $K_1$  and  $K_2$ , the sample can have an easy axis or easy plan.

**Magnetoelastic energy and magnetostriction** is the elastic energy of a magnetic material that arises from the interaction between the magnetization and the strains. Magnetoelastic energy is the increase in the anisotropy energy of magnetic material when submitted to stress. Magnetostriction, the intrinsic property of magnetic material, is the coupling between magnetic and elastic energy, i.e. when subjected to magnetic field magnetic material changes shape [3, 14–16].

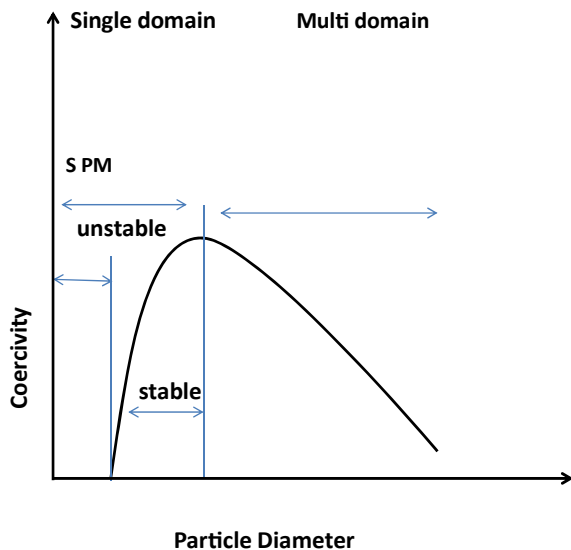
Exchange interaction is responsible for the ordering of atomic magnetic moments which causes the atomic magnetic moments to become parallel and showing magnetic ordering in ferromagnetic material. But the presence of other interactions such as anisotropy, dipolar, magnetoelastic etc. leads to the formation of magnetic domains,

where the magnetic moments are perfectly ordered [3]. As the size of the particle is reduced, the energy necessary to divide itself into magnetic domains is higher than the energy needed to remain as a single magnetic domain or monodomain [10, 17].

The size of the magnetic material has a great influence in determining its magnetic behaviour, e.g. a ferromagnetic material below a critical particle size (15 nm) can possess a single magnetic domain and can show paramagnetic behaviour above a characteristic temperature called blocking temperature ( $T_B$ ). With the increase of the size of the magnet, the number of magnetic domains increases, and as a result, the number of domain walls also increases. During the whole process, there is a decrease in magnetostatic energy while there is an increase in the exchange and the anisotropy energies because of the more number of domain walls [8, 18]. This dependency of magnetic property on the size of the magnetic material can be illustrated by considering the coercivity of the magnet and the dependence of coercivity on the size of the magnet as shown in Fig. 32.2 [3, 16, 19].

For very small particles, with a diameter smaller than the critical diameter of superparamagnetism ( $D_{spm}$ ), the particle shows unstable magnetization with flipping spin and it results in zero coercivity ( $H_c$ ). For the diameter in the range between  $D_{spm}$  and the critical diameter of a single domain ( $D_{sd}$ ), the magnetic moment shows stable nature and hence coercivity ( $H_c$ ) does not become zero. Coercivity increases with the increase of single-domain diameter  $D_{sd}$  and after reaching the multidomain region with the increasing diameter, coercivity again decreases. Hence the magnet shows the maximum coercivity when the diameter is equal to the single-domain diameter,  $D_{sd}$  [8, 10, 20–22].

**Fig. 32.2** Dependency of coercivity on the size of the particle diameter of magnetic nanomaterial



## 32.2 Basic Concept of Superparamagnetism

*Superparamagnetism* (SPM) is a type of magnetism that develops in small nanoparticles of ferromagnetic or anti-ferromagnetic materials which possess single-domain non-interacting magnetic moment grains. Nanosized material with a single magnetic domain can show superparamagnetic behaviour below  $T_B$  (blocking temperature) also when the size is sufficiently reduced below blocking volume ( $V_B$ ), which is the maximum volume below which superparamagnetism starts at a particular temperature and that possibly arises due to spin-based momentum of the unpaired electrons present in the material [21–23].

The energetic stability of a single magnetic domain was theoretically predicted and established by Kittel in 1946 [24]. Magnetic nanoparticles generally show a preference along the direction where magnetic alignment takes place and are said to be anisotropic along these directions. Nanoparticles generally show uniaxial anisotropy, which means that there are two easy directions of magnetization pointing in opposite directions (antiparallel) and are separated by an energy barrier. For single-domain magnetic material, all the magnetic moments are aligned along the preferred anisotropy axis, therefore the free energy contribution from exchange and anisotropy becomes zero. Hence the magnetostatic energy becomes the only relevant energy term.

The critical diameter of the single domain ( $D_{sd}$ ) of magnetic material has a close relationship with the anisotropy constant  $K$ . For identical saturation magnetization ( $M_s$ ) single-domain diameter  $D_{sd}$  increases with domain wall energy, i.e.  $D_{sd}$  is proportional to the domain wall energy. When the size reduction of the particle is sufficiently large then thermal energy overcomes the anisotropy energy. At this stage of magnetization magnetic moment shows fluctuating nature rather than stable nature [8, 20, 21].

At a given temperature, as the size is reduced to a large extent, spin-wave energy modifies and becomes comparable to thermal energy in single-domain non-interacting magnetic grain or particle, and thermal energy becomes insufficient to overcome the spin–spin interaction and can lead to random orientations of magnetic spins inside the particles. The critical diameter  $D_{spm}$  is the maximum size below which the superparamagnetic behaviour starts at a particular temperature and the corresponding volume at which a particle goes from blocked to unblocked state is called blocking volume ( $V_B$ ) [22, 23].

At blocking temperature ( $T_B$ ), thermal energy overcomes the anisotropy barrier of nanoparticles. Above blocking temperature ( $T_B$ ), thermal fluctuations dominate and magnetic moments are randomly orient. Nanoparticles with a uniaxial anisotropy randomly flip the direction of their magnetization and show a spontaneous reversal of magnetization when thermal fluctuation is sufficient enough to overcome the barrier potential that is supposed to arise from magneto crystalline in origin and due to magnetoelastic and shape anisotropy. It was Neel [25] who shows that above  $T_B$  a stable magnetization cannot be established due to thermal fluctuations acting on small particles, and as a result, the system shows *superparamagnetic* behaviour. The

typical time of average laps between two flips is called *Neel-relaxation time*  $\tau_N$ . If  $\tau_m$  is considered to be the measuring time of the magnetic effect of a particular nanomagnetic material for its observed magnetic behaviour, then the following observations can be made in a nanomagnetic material [25, 26].

If  $\tau_m < \tau_N$ , the material is in a blocked state and the magnetization flip does not take place.

If  $\tau_m > \tau_N$ , magnetic flip occurs and magnetic behaviour alters. The material shows superparamagnetism.

This shows that the observed magnetic behaviour in nanomagnetic material depends on measuring time  $\tau_m$ . In most practical applications the measuring time  $\tau_m$  is tried to keep constant. The transition between superparamagnetic and blocked state is used to study as a function of applied temperature.

The first and basic theory that describes the basic understanding of nanoparticle magnetism is the *Stoner-Wolfforth model* [14, 27]. In this model, each nanoparticle is considered as an ellipsoidal homogenous single-domain non-interacting grain. According to this theory, depending on the spin configuration nanoparticles may have a single domain, vortex or multidomain state. Nanoparticles in the smallest range of diameter do not behave as stable magnet but exhibit the phenomenon of superparamagnetism [3]. However, this model is suitable at  $T = 0$  K and is applicable to nanoparticles with uniaxial anisotropy only. The large surface to volume ratio in nanoparticles enhances the magnetic moment and anisotropy [27].

### 32.2.1 Basic Theory

The energy expression for single-domain magnetic grain with uniaxial anisotropy in the presence of external magnetic field  $H$  can be expressed as the sum of magnetic anisotropy energy and Zeeman energies:

$$E = KV \sin^2 (\Phi - \theta) - \mu_0 M_s V H \cos \Phi \quad (32.3)$$

where  $V$  is the grain volume of the nanoparticle,  $K$  being the uniaxial anisotropy constant parameter and  $M_s$  is the saturation magnetization. All the three quantities, external magnetic field  $H$ , grain magnetization and magnetization easy axis lie in the same plane.  $\Phi$  represents the angle between magnetization and magnetizing field and  $\theta$  represents the angle between magnetization easy axis and magnetizing field [10, 17, 25, 28].

In absence of an external magnetic field, two equally energetically favourable directions exist. Both directions are parallel to the energetically favourable spontaneous magnetization direction also called magnetization easy axis for anisotropic magnetic material and there possess the energy barrier  $\Delta E$  between them in  $KV$ . At temperatures higher enough, the thermal energy  $kT$  is capable of overcoming the



barrier potential and alteration of magnetization direction takes place. While in presence of an external magnetic field, the symmetry of the two magnetization easy axis directions breaks down. When magnetization direction is along the external magnetic field, domain energy of the nanoparticle grain decreases and therefore energy barrier for spin fluctuation becomes high. The reverse is the case when magnetization directs in opposite direction to an externally applied magnetic field, the energy barrier for spin fluctuation decreases and reversal of magnetization takes place spontaneously. So nanoparticles with uniaxial anisotropy flip the direction of their magnetization randomly and spontaneously. The thermally initiated fluctuations of the magnetization direction between the two easy axis directions are called *superparamagnetic (Neel) relaxation* and the typical expression for *Neel-relaxation time*  $\tau_N$  can be expressed by the Neel-Brown expression as

$$\tau_N = \tau_0 \exp(\Delta E / kT) \quad (32.4)$$

where  $\tau_0$  is the length of time and is the function of the characteristic of the material and usually lies between  $10^{-12}$  s and  $10^{-9}$  s.  $\tau_0$  depends weakly on temperature and various material parameters such as magnetic anisotropy constant, particle volume and saturation magnetization [10, 16, 17, 25, 28].

In this regard, a definition of blocking temperature  $T_B$  can be given as the temperature at which the relaxation time  $\tau_N$  equals the experimental time  $\tau_m$  or  $T_B$  can be defined as the temperature between the blocked and the superparamagnetic state [25, 28].

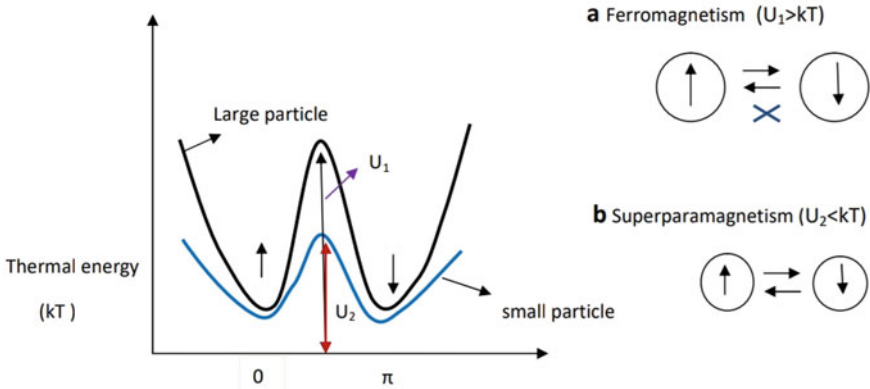
Equation (32.4) represents the connection between the time  $\tau_N$  and the temperature  $T$ .

$$\text{At } \tau_N = \tau_m \quad T_B = \Delta E / k \ln(\tau_m / \tau_0), \quad (32.5)$$

A clear distinction between the two states can be expressed as

- The state is blocked when  $\tau_m < \tau_N$  or  $T < T_B$ .
- The state becomes superparamagnetic when  $\tau_m > \tau_N$  or  $T > T_B$ .

The first reveal of single-domain particle magnetization presented by *Stoner* and *Wohlfarth* [14] suggested the existence of high coercivity fields below  $T_B$ . The anisotropy energy arising from magnetocrystallogenic origin becomes comparable to thermal energy and the direction of the magnetic moment starts fluctuating spontaneously and goes through a rapid superparamagnetic relaxation. The supposed system of uniform non-interacting nanoparticles at  $T > T_B$  overcomes barrier energy and the magnetic moments started flipping between the easy magnetization directions. At  $T < T_B$ , the magnetocrystalline-originated anisotropy energy barrier cannot be overcome by the thermal energy and the magnetic moment of each particle rotates from the field direction back to the nearest easy magnetization axis because of which non-zero coercivity results. The total magnetization decreases with increasing temperature as the nanoparticles and the corresponding easy magnetization directions are randomly



**Fig. 32.3** Ferromagnetism in large and small magnetic particle, **a** large particle magnetism ( $U_1 > kT$ ), no spin flipping takes place, **b** small particle superparamagnetism ( $U_2 < kT$ ), with spin flipping

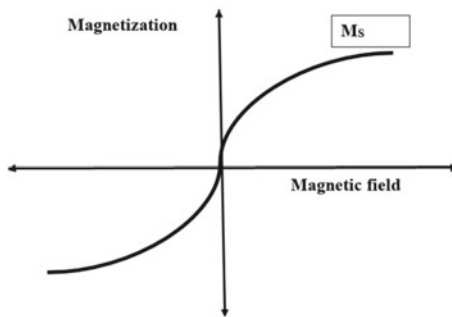
oriented and the randomness increases with temperature [20, 21, 28]. Figure 32.3 shows the ferromagnetism in large particles and superparamagnetism in small nanoparticles.

### 32.3 Brief Discussions

The typical behaviour of large particle ferromagnetism and small particle ferromagnetism can be observed from the thermal energy transition curve. For two vectors spin directions (vector upward  $\uparrow$  and vector downward  $\downarrow$ ), if spin vector cannot move from one direction to other, there exist some net magnetization and the material shows ferromagnetism, i.e. when exchange energy  $U_1 > kT$  vector spin cannot flip or re-orient. In the energy plot (thermal energy as a function of the orientation of the spin) if one spin magnetic moment vector lies in the first stability zone (minimum energy) and if it has to come to the next stability zone (with minimum energy) it has to overcome the energy barrier. The energy barrier is proportional to the grain particle volume ( $V$ ). The energy barrier potential for a large particle is large. If the spin has to change its direction it has to overcome the large energy barrier. For a small-sized particle of nanodimension, this energy difference is much smaller; therefore, it is easy for the magnetic vector to change its direction crossing the potential barrier. At room temperature also the thermal energy is much greater than the exchange energy between the magnetic vectors [10, 28].

Hence for large particles, at room temperature, the thermal energy is much less than the energy required to cross the barrier, but this energy is sufficiently more than the energy required crossing the barrier in small particles changing the magnetic vector. Hence there is an automatic reversible change in the direction of magnetic vector or spin. At normal temperature also this spin flipping can take place in a

**Fig. 32.4** Curve showing superparamagnetism with remanence  $M_R = 0$  and  $H_C = 0$



nanodimensional particle; hence both the possibilities of stable state are possible in the system. This spin flipping leads to the property of superparamagnetism in the nanosystem. Whenever the energy required or exchange energy  $U_2$  is less than  $kT$  (thermal energy) then it can have spin fluctuation and it results in superparamagnetism. Figure 32.4 presents the typical behaviour of the superparamagnetism nature of magnetic nanoparticles, where the magnetization curve passes through the origin.

## 32.4 Conclusions

For large particle, the hysteresis loop possesses a particular area. When the particle size is reduced sufficiently (around 10–12 nm), these particles do not show the hysteresis loop but a plot that goes through the origin, which is like both remanence and coercive field are zero. This represents the typical paramagnetic behaviour. Although these particles are small they have several moments comprising ions or molecules. These moments are flipping among themselves and the resultant is a paramagnetic behaviour. This is one of the important aspects of the magnetic properties of nanostructures [29]. When the particle size is large it shows the hysteresis loop, but for the same material particle when the size is reduced to nanodimension it does not show hysteresis but passes through the origin with no remanence and coercive field, i.e. superparamagnetism is a function of the size of the particle.

## References

1. D.J. Sellmyer, M. Zheng, R. Skomski, *J. Phys.: Condens. Matter.* **13**(25), R433 (2001)
2. J.P. Liu, E. Fullerton, O. Gutfleisch, D.J. Sellmyer, Springer Science +Business Media, LLC, (2009)
3. A.P. Guimaraes, *Principles of Nano Magnetism*, NanoScience and technology, ISBN 978–3–642–01481–9
4. C.Z. Wu, P. Yin, X. Zhu, C OuYang, Y Xie, *J. Phys. Chem. B* **110**(36), 17806 (2006)
5. D. Kim, N. Lee, M. Park, B.H. Kim, K. An, T. Hyeon, *J. Am. Chem. Soc.* **131**, 454 (2009)

6. C. Moya, A.M. Abdelgawad, N. Nambiar, S.A. Majetich, *J. Phys. D: Appl. Phys.* **50**(32), 325003 (2017)
7. M.V. Kovalenko, M.I. Bodnarchuk, R.T. Lechner, G. Hesser, F. Schaffler, W. Heiss, *J. Am. Chem. Soc.* **129**, 6352–6353 (2007)
8. C. Yang, Y.L. Hou, S. Gao, *Chin. Phys. B* **23**(5), 057505 (2014)
9. L.H. Zhang, J.J. Wu, H.B. Liao, Y.L. Hou, S. Gao, *Chem. Commun.* **454**, 378 (2009)
10. M. Knobel, W.C. Nunes, L.M. Socolovsky, E.D. Biasi, J.M. Vargas, J.C. Denardin, *J. Nanosci. Nanotechnol.* **8**(6), 2836–2857 (2008)
11. R.A. Lukaszew, *Hand Book of Nanomagnetism Application and Tools*, (Jenny Stanford Publishing, 2015)
12. J. Shen, J. Kirscher, *Surf. Sci.* **500**, 300 (2002)
13. N.A. Spaldin, *Magnetic Materials Fundamentals and Device Applications*, (Cambridge University Press, New York, 2003), ISBN 0-521-81631-9
14. G. Schmid, (ed.), *Nanoparticles: From Theory to Application*, WILEY-VCH Verlag
15. GmbH & Co. KGaA, (2004)
16. M. Knobel, W.C. Nunes, A.L. Brandl, J.M. Vargas, L.M. Socolovsky, D. Zanchet, *Phys. B: Condens. Matter* **354**(1–4), 80–87 (2004)
17. J.M. Vargas, W.C. Nunes, L.M. Socolovsky, M. Knobel, D. Zanchet, *Phys. Rev. B* **72**(18), 184428 (2005)
18. B.D. Cullity (ed.), *Introduction to Magnetic Materials* (Addison-Wesley Publishing Co., Reading, Massachusetts, 1972)
19. G.C. Hadjipanayis, *J. Magn. Magn. Mater.* **200**, 373 (1999)
20. C.H. Chen, S.J. Knutson, Y. Shen, R.A. Wheeler, J.C. Horwath, P.N. Barnes, *Appl. Phys. Lett.* **99**, 012504 (2011)
21. D. Goll, A.E. Berkowitz, H.N. Bertram, *Phys. Rev. B* **18**, 184432 (2004)
22. C. Yang, J.J. Wu, Y.L. Hou, *Chem. Commun.* **47**, 5130 (2011)
23. J.L. Dorman, D. Fiorani, E. Trone, *Adv. Chem. Phys.* **98**, 283 (1997)
24. C. Bean, J.D. Livingston, *J. Appl. Phys.* **30**, 120S (1959)
25. C. Kittel, *Phys. Rev.* **70**, 965 (1946)
26. L. Neel, *Ann. Geophys.* **5**, 99 (1949)
27. W.C. Nunes, W.S.D. Folly, J.P. Sinnecker, M.A. Novak, *Phys. Rev. B* **70**, 014419 (2004)
28. E.C. Stoner, E.P. Wohlfarth, *Philos. Trans. R. Soc. A* **240**, 599 (1948)
29. W.C. Nunes, L.M. Socolovsky, J.C. Denardin, F. Cebollada, A.L. Brandl, M. Knobel, *Phys. Rev. B* **72**, 212413 (2005)